



**Answer the following questions**

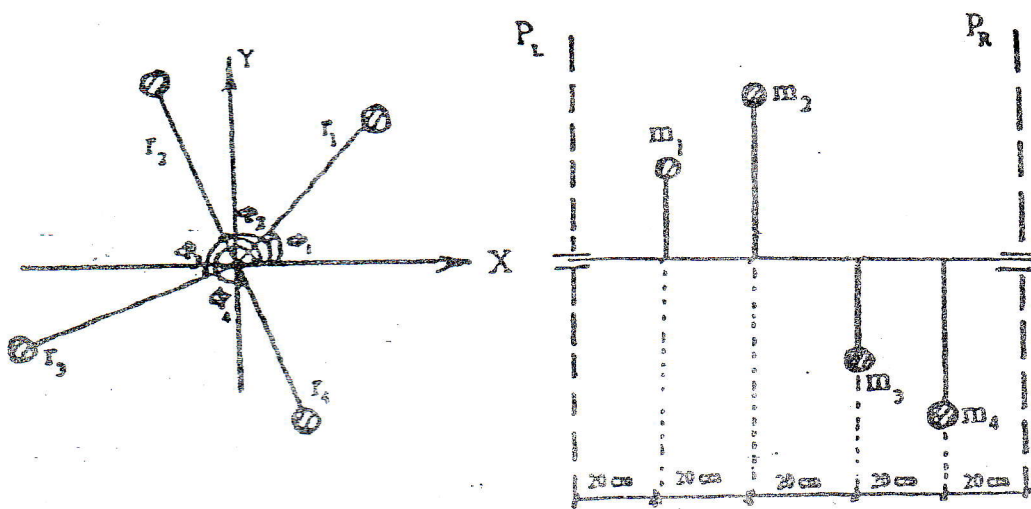
**Question 1**

**(30 marks)**

(A) Write short notes on:

- i) Basic concepts of vibration
- ii) Classification of vibration
- iii) Mass (inertia) elements
- iv) Damping elements
- v) Harmonic motion

(B) A shaft with four unbalanced masses should be completely balanced by two masses situated on the radius  $r_0$  in two respective planes  $\delta_L$  and  $\delta_R$  as shown, find these masses  $m_L$  and  $m_R$  as well as their angular locations  $\phi_L$  and  $\phi_R$ .



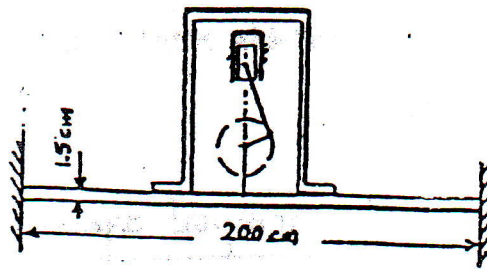
**Question 2**

**(40 marks)**

(A) A reciprocating engine, weighting 75 kg, is mounted at middle of a steel plate of thickness 1.5 cm, width 40 cm and length 200 cm, clamped along two edges as shown in figure. If  $E = 2.114 \times 10^6 \text{ kg/cm}^2$  during the operation of the engine, the plate is subjected to a harmonic unbalanced vertical force:

$$F(t) = 1000 \sin 80 t \text{ N}$$

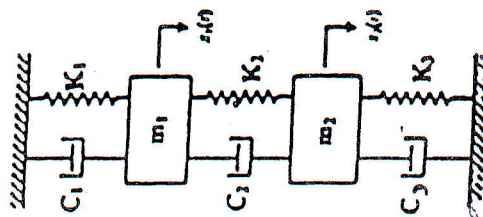
- i) Determine the steady-state amplitude and if the damping is introduced with damping factor 0.3 to the system, determine the steady state amplitude,
- ii) In the absence of the damping, design the proper undamped dynamic absorber to be fitted to the system in order to obtain zero amplitude ( $r_1$ ) of machine, and also the corresponding amplitude ( $r_2$ ) in this case, taken into the account the mass ratio is  $1/3$ .



**(B)** The shown system in figure performs small vibration about its stable equilibrium position.

Given  $K_1 = K_2 = 0.5 K_3 = 10.000 \text{ N/m}$ , and  $C_1 = C_2 = C_3 = 2000 \text{ N-s/m}$ ,  $2 m_1 = m_2 = 2 \text{ kg}$ , Determine:

- i) Derive the equations of motion of the system,
- ii) Determine the natural frequencies and mode shapes, and sketch these modes, then check the correctness of the results.



**Question 3****(30 marks)**

- (A) The governing equation of a uniform Bernoulli-Euler beam under pure bending resting on fluid layer under axial force is:

$$EI \frac{\partial^4 v}{\partial x^4} + p \frac{\partial^2 v}{\partial x^2} + k_f v + F(x, t) = 0, \quad 0 \leq x \leq L_e.$$

with boundary conditions (Clamped-Simply supported):

$$\text{at } x = 0, \quad W(x) = \frac{dW(x)}{dx} = 0$$

$$\text{at } x = L_e, \quad W(x) = \frac{d^2W(x)}{dx^2} = 0$$

Solve the Riccati equation problem using the adomian decomposition method (ADM). Then compared the results with exact solutions.

- (B) The governing equation of a non-uniform Bernoulli-Euler beam under axial force resting on fluid layer is:

$$\rho A \frac{\partial^2 v}{\partial t^2} + p \frac{\partial^2 v}{\partial x^2} + k_f v + \frac{\partial^2}{\partial x^2} \left( E I \frac{\partial^2 v}{\partial x^2} \right) = 0, \quad 0 \leq x \leq L_e.$$

For any combination of the clamped and simply supported conditions at the two ends

Solve using the adomian decomposition method (ADM).

This exam measures the following ILOs										
Question Number	Q1-1	Q1-2	Q1-3	Q1-4	Q3-1,2,3	Q4-1,2,3			Q2-a	Q2-b
Skills	Q1-5									
	Knowledge & understanding skills				Intellectual Skills				Professional Skills	

*With my best wishes*

*Dr. Eng. Ramzy M. Abumandour*